Cryptographic Schemes Based on the ASASA Structure: Black-box, White-box, and Public-key

A. Biryukov, C. Bouillaguet, D. Khovratovich, (talk given by Ivica Nikolic)

University of Luxembourg and University of Lille

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Secret-key White-box Public-key

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White-box cryptography (WBC) Motivation for the ASASA construction in public- and secret-key schemes

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WBC centers around *white-box implementation*:

- 1. Pure software implementation of a cipher (encryption or decryption routine) with *embedded key*;
- 2. Implementation is assumed available to an adversary.
- 3. Weak white-box: Adversary can not extract the *key* from the implementation.

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Example: recovering protected media content, which is decoded in software:



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- 3. **Strong white-box**: adversary can not *invert* the cipher, i.e. can not decrypt given the encryption routine.

Similar to public-key cryptography. Why not using it?

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Similar to public-key cryptography. Why not using it?

- RSA-2048 encryption speed 1000 cycles per byte.
- AES-128 encryption speed 0.7 cycles per byte.

Impractical for large amount of data (HD movies, etc.).

Failure to build weak white-box with AES

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How to white-box a cipher:

- Replace key-dependent transformations with lookup tables;
- Encode the encryption as a sequence of lookups.



SQA

AES-128 (designed in 1997, adopted in 2001): 10-round cipher with 16-byte state.

- One round of AES:
 - Four 32-bit blocks:
 - AddRoundKey (simple XOR);
 - SubBytes (bytewise nonlinear);
 - MixColumns (linear).
 - ShiftRows (byte permutation).



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White-boxing AES round

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- Wrap the key addition and S-boxes with redundant linear and nonlinear transformations;
- The secret layers collapse to the SAS structure.
- Replace every 32-bit block with a lookup table;
- Store everything in memory.

Actual proposal used smaller and weaker tables.

The SAS structure has some exploitable properties:



- For instance, set (*, C, C, C) transforms to (D, D, D, D).
- This led way to various sorts of attacks, including differential and algebraic ones.
- Outer layers can be retrieved.

Constructions as large as SASAS are vulnerable [Biryukov-Shamir'01].

ASASA

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However, the ASASA structure is still unbroken:



Hints for new designs...

Our contributions

Secret-key ASASA

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ASASA

Symmetric ASASA with secret layers.



- Key-dependent affine layers (random invertible matrices);
- Key-dependent secret 8-bit S-boxes (random permutations);
- We estimate 128-bit security for 128-bit keys and 128-bit blocks;
- Some attacks on other parameters are presented in the paper.

White-box ASASA

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Weak white-box: adversary can not extract the *key* from the implementation.



We extend the definition: it should be infeasible to derive a key or *any other compact secret* from the WB implementation.

Adversary can not recover the components \implies he has to use/broadcast the implementation "as is".

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Our solution for weak white-box security: an implementation that *can not be compressed*.

Consider small block (\leq 32 bits) ASASA cipher and encode it as a lookup table.



Incompressible implementation



- Cipher composed of smaller *d*-bit subciphers ($8 \le d \le 28$).
- Parameter *d* determines the implementation size.
- Subcipher invocations alternate with public permutations (*L*).
- Total implementation size can be tuned from 2 MB to 20 GB.

Public-key and strong white-box ASASA

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Public-key cryptography with polynomials (dates back to 1980s):

$$\mathbf{b} = A_2 \circ \mathbf{S} \circ A_1, \tag{1}$$

where A_1 and A_2 are key-dependent and secret affine transformations, and **S** is a public invertible polynomial of degree 2.

• Degree-2 polynomials of 128 boolean variables are compact enough (less than 1 MByte), and there is no generic inversion algorithm.

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- Degree-2 polynomials of 128 boolean variables are compact enough (less than 1 MByte), and there is no generic inversion algorithm.
- However, virtually all variants of this scheme have been broken because of properties of **S**: only a few families of invertible polynomials are available (even without trapdoors).

How about adding more layers to get ASASA?

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Asymmetric scheme

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Polynomial-based S-boxes of degree 2?



The encryption function is a set of degree-4 polynomials.

Asymmetric scheme

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First attempt: use Daemen's nonlinear function $(y_i = x_i \oplus x_{i+1}x_{i+2} \oplus x_{i+2})$, used in Keccak/SHA-3.



Problems:

- Broken with Grobner basis attacks in real time;
- Also vulnerable to generic decomposition algorithms [Faugere-Perret'10];

Our solution: ASASA with expanding S-boxes and perturbation (noise):

$$\mathbf{b} = U \circ \mathbf{a}_2 \circ T \circ \mathbf{a}_1 \circ S$$

- Two nonlinear layers (128 \rightarrow 256 and 256 \rightarrow 512 bits);
- Nonlinear transformations are expanding and more random-looking;
- Perturbation (a₃) added to defeat generic decomposition algorithms;
- 24 MBytes of public key.



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Additional material in the proceedings and on ePrint:

- LPN and algebraic attacks on weakened multivariate schemes;
- Various attacks on secret-key ASASA.

Questions?